

6)

$$\frac{p}{q} = 1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots - \frac{1}{1318} + \frac{1}{1319}$$

Consider now $\frac{p}{q}$ irreducible ($\gcd(p, q) = 1$)

$$\frac{p}{q} = \left(1 + \frac{1}{3} + \frac{1}{5} + \frac{1}{1319}\right) - \left(\frac{1}{2} + \frac{1}{4} + \frac{1}{6} + \dots + \frac{1}{1318}\right)$$

$$\frac{p}{q} = \left(1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{1318} + \frac{1}{1319}\right) -$$

$$= 2\left(\frac{1}{2} + \frac{1}{4} + \frac{1}{6} + \dots + \frac{1}{1318}\right)$$

$$\frac{p}{q} = \left(\cancel{1} + \cancel{\frac{1}{2}} + \cancel{\frac{1}{3}} + \frac{1}{1319}\right) - \left(\cancel{1} + \cancel{\frac{1}{2}} + \cancel{\frac{1}{3}} + \dots + \cancel{\frac{1}{1319}}\right)$$

$$\frac{p}{q} = \frac{1}{660} + \frac{1}{661} + \dots + \frac{1}{1319}$$

$$\frac{p}{q} = \left(\frac{1}{660} + \frac{1}{1319}\right) + \left(\frac{1}{661} + \frac{1}{1318}\right) + \dots + \left(\frac{1}{989} + \frac{1}{990}\right)$$

$$\frac{p}{q} = \frac{1979}{660 \cdot 1319} + \frac{1979}{661 \cdot 1318} + \dots + \frac{1979}{989 \cdot 990}$$

$$\frac{p}{q} = 1979 \left(\underbrace{\frac{1}{660 \cdot 1319} + \frac{1}{661 \cdot 1318} + \dots + \frac{1}{989 \cdot 990}}_{\frac{a}{b}} \right)$$

$$\text{mcd}(a, b) = 1$$

$$p \cdot b = 1979 \cdot a \cdot q$$

Como 1979 es primo o bien $p = 1979$

o bien $b = 1979$, pero $b = \text{mcm}(660, \dots, 990)$

y por tanto no es múltiplo de 1979

$$\rightarrow \boxed{p = 1979}$$